Where do the platelets go? A simulation study of fully resolved blood flow through aneurysmal vessels

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Despite the importance of platelets in the formation of a thrombus, their transport in complex flows has not yet been studied in detail. In this paper we simulated red blood cells and platelets to explore their transport behaviour in aneurysmal geometries. We considered two aneurysms with different aspect ratios (AR = 1.0, 2.0) in the presence of fast and slow blood flows (Re = 10, 100), and examined the distributions of the cells. Low velocities in the parent vessel resulted in a large stagnation zone inside the cavity, leaving the initial distribution almost unchanged. In fast flows, an influx of platelets into the aneurysm was observed, leading to an elevated concentration. The connection of the platelet-rich cell-free layer (CFL) with the outer regions of the recirculation zones leads to their increased platelet concentration. These platelet-enhanced recirculation zones produced a diverse distribution of cells inside the aneurysm, for the different aspect ratios. A thin red blood CFL that was occupied by platelets was observed on the top of the wide-necked aneurysm, whereas a high-haematocrit region very close to the vessel wall was present in the narrow-necked case. The simulations revealed that non-trivial distributions of red blood cells and platelets are possible inside aneurysmal geometries, giving rise to several hypotheses on the formation of a thrombus, as well as to the wall weakening and the possible rupture of an aneurysm.

1. Introduction

Intracranial aneurysms are pathological dilatations of the cerebral blood vessels with high mortality and morbidity rates associated with their possible rupture. One repair mechanism is the formation of a thrombus inside the aneurysm, significantly lowering the risk of rupture [1,2]. This formation can also be induced by positioning a flow-diverting stent in the orifice of the aneurysm. Quantitative models of thrombosis in intracranial aneurysms are now needed, and the European Union-funded project THROMBUS aims to validate such models and translate them into clinical practice [3].

Platelets, or thrombocytes, are the main component of a thrombus. They exhibit excess concentration near the walls of a vessel [4–6], ensuring a more effective response to wounds and tissue damage. This margination is amplified by the shape and dynamics of red blood cells (RBCs) [4–7], and a similar behaviour can be observed for white blood cells [8]. The presence of RBCs is also important in the adhesion and aggregation of platelets, based on computational studies [9,10]. Almost all thrombosis models that have been developed [11–14] and applied to aneurysm geometries [15–18] treat platelets on a mean field level, by modelling them as tracer particles in a homogeneous fluid.

Several methods have been proposed and used to describe the transport of platelets in blood flow. A simple approach for the transport is by using an advection–diffusion model, with a simple scalar diffusion term as used in recent studies [12,16]. Modelling the transport of platelets with scalar diffusion in an incompressible fluid without sources and sinks will eventually lead to a...
homogeneous distribution [19]. Eckstein & Belgacem [20] proposed an additional drift term to mimic RBC enhanced motion, whereas more sophisticated approaches involving the explicit dependence of the diffusion coefficient on the local haematocrit and shear rate have also been proposed [21,22]. The dependence on these quantities has already been recognized in early experimental work [4,23]. Although such methods may provide adequate results in simple channel flows, little is known about the behaviour of platelets in more complex flow geometries, in which most of these models lack validity [24]. The research on the modelling of thrombosis to date mainly uses advection–diffusion descriptions at the macroscopic scale for the transport of platelets, without taking full account of the non-trivial nature of the presence of RBCs in the transport, especially in more complex geometries.

Simulations with fully resolved RBC and platelet suspensions are challenging, owing to the computational cost of considering thousands or even millions of particles. Smaller scale studies of blood flow are preferred for qualitative studies. For example, Crowl & Fogelson [25,26] simulated the lateral motion of platelets in a two-dimensional channel, whereas three-dimensional studies have focused on varying parameters and examining their effect on the margination [27,28]. At this cellular scale, models have either emphasized flows in straight channels or used a haematocrit significantly lower than the physiological value. In this article, we focus on investigating the transport behaviour and the distribution of platelets in aneurysmal geometries by explicitly simulating platelet-sized and deformable membraneous RBC-shaped particles in suspensions with physiological haematocrit values. The aim is to explore the behaviour of platelets in complex flows, and give insights into the formation of thrombus in aneurysms by understanding where the platelets are located in aneurysmal geometries.

2. Methods and model

Blood is a multi-phase non-Newtonian fluid consisting of RBCs, platelets and white blood cells suspended in plasma, a protein-rich Newtonian fluid. The complex behaviour of blood mainly arises from the high concentration of RBCs, which constitute up to 45 per cent of the total blood volume. Our approach fully resolves deformable RBCs and platelet-shaped particles, suspended in the plasma. A two-dimensional approach has been used, using the lattice Boltzmann method (LBM; [29]) as a fluid solver and coupled to a discrete element representation of the cells using the immersed boundary method (IBM; [30]).

The LBM is a well-established mesoscopic approach, solving the incompressible Navier–Stokes equation, and has demonstrated capabilities in many studies of biomedical interest [12,31–34].

The IBM is a fluid structure interaction method in which a membrane is immersed in the fluid. The idea behind the IBM is to advect the elements of the membrane with the fluid, based on the no-slip condition. The forces between the membrane elements are applied back to the fluid. The IBM is a pure coupling method with a small numerical overhead and is one of the most widely used methods to couple RBC-like structures with fluid flow in two dimensions [26,35–37] and in three dimensions [38,39].

2.1. Blood model

Modelling blood through its constituents allows important rheological and transport properties to be captured, without the simplifications that would be necessary for a macroscopic approximation.

The D2Q9 LBGK scheme is used to simulate the fluid flow [29], whereas the viscosity is chosen to match blood plasma [40]. RBCs are represented as a closed deformable membrane with a bicone shape and a diameter of 8 µm. Circular-shaped cells with a diameter of 2 µm, slightly deformable, constitute the platelet-sized particles. Our ‘platelets’ are not reactive and do not adhere or aggregate, but correspond to the platelet-sized passive particles found in in vitro studies [4,6,41].

The membrane of the cells is represented with neighbouring surface points connected with Hookean springs and enhanced with bending resistance between the adjacent membrane springs. The viscous properties of the membrane derive from damper elements connecting surface points, while the conservation of volume and surface is ensured by applying forces in an equivalent way to the pressure differences between the inner and surrounding fluid of the membrane. Similar models and implementations can be found in recent studies [26,35,37].

The model is tuned such that the single-cell dynamics are resolved sufficiently in the range of shear rates of interest [42]. A repulsion force is also included to overcome artificial correlation resulting from the IBM interaction and is tuned to the extent that the shear-thinning behaviour is correctly recovered. Shear thinning results naturally from the deformability of the RBC shape and the formation of rouleaux-like structures at lower shear rates [43].

A balance is necessary between resolving important aspects of the flow field around a RBC-shaped particle and avoiding the heavy computations owing to the diffusive scaling of the LBM. Our approach is aiming for the simplest possible model that reproduces important aspects of rheology and single-cell dynamics. It has been validated against various benchmarks, such as tumbling and tank-treading transition of a single RBC in shear flow, the shear-thinning behaviour and the haematocrit dependence of blood viscosity (data not shown; for details see [42]). Figure 1 illustrates a snapshot from a simulation of the flow through an aneurysm geometry, demonstrating the model representation of the cells along with two magnifications.

With the current model, we investigate the three-dimensional process of cell transport in blood flow, limited to two dimensions. The distributions of cells inside two-dimensional aneurysms may differ significantly from three-dimensional idealized cases, because no obvious symmetry exists. In many respects, however, the behaviour of a two-dimensional suspension system is similar to that in a three-dimensional system, particularly in terms of the quantities and effects that interest us in this work [26,27]; thus we are able to maintain the main advantage of a two-dimensional simulation, i.e. reduced computational requirements.

2.2. Simulation set-up

The fluid was initially allowed to rest and then it was driven by a constant body force, mimicking a pressure gradient. The pulsatility of the flow was neglected owing to the relatively small Womersley number $Wo = L\sqrt{\omega/v}$, $L$ being the
characteristic length scale, $\omega$ the angular frequency of the oscillations and $\nu$ the kinematic viscosity. For intracranial arteries, typically $Wo \approx 3.2$. Instead, two different Reynolds numbers, $Re = LU/\nu \approx 10$ and 100, were considered, in order to approximate two different situations within the cardiac cycle ($U$ is the characteristic velocity). The total simulated time was 0.2 s. Reynolds numbers were calculated based on the size of the parent vessel, the plasma viscosity and the imposed pressure gradient, supposing a Poiseuille profile without RBCs. Owing to the suspension of RBCs and the aneurysm bulge, the final resulting velocity will be slightly different.

First, we consider the case of a straight channel and compare our results with those of in vitro experiments, recovering the transport properties of platelets in a tube in the presence of RBCs. Next we consider two aneurysmal geometries with different aspect ratios in order to study the cell transport in more complex flows, exposing the fluid to two different pressure gradients. The aspect ratio is defined as the ratio of the maximum perpendicular height to the average neck diameter [44] and has been identified as an important parameter for rupture [45] and for the formation of a thrombus in an aneurysm.

We have chosen to use the geometries introduced in recent studies [11,16] in order to compare our fully resolved model with simulations in which blood was modelled as a continuous Newtonian fluid. The four cases are named after the geometry acronym and the Reynolds number: LLa100, LLa010, Sa100 and Sa010, and details of the geometrical parameters can be found in table 1. Similar flow patterns to the studies reported earlier were found by using the same Reynolds number, but the smaller size of the vessel caused higher absolute velocities and shear rates. The diameter of the main vessel is 0.1 mm, close to 10 times smaller than those found in human cerebral arteries [46]. The dimensions of the domain were preferred in order to reduce the computational cost of each simulation, because a factor of 10 in diameter would yield a factor of 100 in the number of lattice nodes and cells.

The initial positions of RBCs and platelets were chosen at random without any overlaps, providing a homogeneous initial distribution. Both fluid and cells were subjected to periodic boundaries. The number of RBCs corresponds to the haematocrit under physiological conditions (42%). Haematocrit is defined as the volume ratio of RBCs to blood. The number of platelets was selected close to the physiological ratio of RBCs to platelets of $15$, ranging from $11$ to $16$, providing a suspension slightly richer in platelets for better statistics.

### 2.3. Quantities of interest

Besides flow fields, velocity and shear rates, the concentration of RBCs and the local concentration of platelets $C_{plt}$ are of particular interest in this study. As the ‘normalized platelet concentration’, we define the ratio of the local platelet concentration to the mean platelet concentration

$$\frac{C_{plt}}{C_{mean}} = \frac{C_{plt}}{C_{mean}}.$$  

where $C_{plt}$ is the local concentration of platelets and $C_{mean}$ is the mean platelet concentration. A normalized platelet concentration equal to 1.0 corresponds to the mean concentration.

The results presented here are the outcome of 15 simulations with different initial conditions. The simulation results are time averaged over the last 0.08 s of the total 0.2 s. The parameters and the settings of the simulations are reported in table 2.

### 3. Results

First, we present the results obtained on a straight channel with a haematocrit equal to 42 per cent and a platelet-only case. This provides a benchmark for the simulated transport. Next, we investigate the transport of platelets and RBCs in two aneurysmal geometries under higher and lower pressure gradients.

#### 3.1. Transport in a straight channel

Results from the straight channel with a haematocrit of 42 per cent are shown in figure 2. The excess of platelets near the walls of the channel is evident, as well as the clearly visible red blood cell free layer (CFL). The formation of a CFL is the microscopic phenomenon behind the Fähnle-Lindqvist effect, which is characterized by a decrease in the apparent blood viscosity as the vessel diameter decreases below 500 $\mu$m [47].

The peak of the RBC concentration in the centre of the channel is a result of the symmetry of the simulated channel, also observed by Zhao & Shaqfeh [48]. Such a peak is not observed under experimental conditions, where higher mixing is expected.

In the absence of RBCs, the distribution of platelets is not homogeneous as would have been expected for Brownian point particles. Platelets tend to crowd around approximately
60 per cent of the radius of the channel. This effect is known from dilute rigid sphere suspensions as the Segré–Silberberg\cite{49} or tubular pinch [5] effect and is a balance of viscous drag and inertial lift forces [50]. Our results are similar to the in vitro profiles of Aarts et al. [5], shown in figure 3. The in vitro data reported by Aarts et al. show a dependency on the wall shear rate, probably due to the insufficient equilibration in the low shear rate cases. This is also true for the profiles obtained in our simulations 1.0 s after the initialization with a homogeneous distribution (blue curve in figure 3).

### 3.2. Transport in aneurysmal geometries

We examined the transport of platelets in aneurysms with different aspect ratios, under high and low pressure gradients.

### 3.3. Lower velocities

The imposed pressure gradient yields a maximum velocity of $u_{\text{max}} \approx 6 \text{(cm s}^{-1})$ in the parent vessel. Significantly lower velocities are observed inside the aneurysm for both aspect ratios (figure 4). Examining the velocity field and the distribution of haematocrit and platelets, we can distinguish three zones for Sa010: (i) the parent vessel, (ii) a circulation zone close to the entrance of the aneurysm, and (iii) a large stagnation zone where cells move really slow. The stagnation zone occupies most of the aneurysm.

Two zones are clearly visible in LLa010: (i) the region of the flow entering the aneurysm and (ii) a large stagnation zone. Close to the entrance of the aneurysm, we observe a region with a depletion of RBCs and occupied by platelets. A recirculation zone is absent from this case.

### Table 1.

Geometrical parameters and set-up of the aneurysm cases. $N_{\text{RBC}}$ is the number of red blood cells and $N_{\text{plt}}$ the number of platelets.

<table>
<thead>
<tr>
<th>case ID</th>
<th>Reynolds number</th>
<th>geometry</th>
<th>aspect ratio</th>
<th>neck size (mm)</th>
<th>$N_{\text{RBC}}$</th>
<th>$N_{\text{plt}}$</th>
</tr>
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<tbody>
<tr>
<td>LLa100</td>
<td>$\approx 100$</td>
<td>LLa</td>
<td>1.0</td>
<td>0.2</td>
<td>4900</td>
<td>300</td>
</tr>
<tr>
<td>LLa010</td>
<td>$\approx 10$</td>
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<td>2.0</td>
<td>0.1</td>
<td>4700</td>
<td>300</td>
</tr>
<tr>
<td>Sa100</td>
<td>$\approx 100$</td>
<td>Sa</td>
<td>2.0</td>
<td>0.1</td>
<td>4700</td>
<td>300</td>
</tr>
<tr>
<td>Sa010</td>
<td>$\approx 10$</td>
<td>Sa</td>
<td>2.0</td>
<td>0.1</td>
<td>4700</td>
<td>300</td>
</tr>
</tbody>
</table>

### Table 2.

Simulation parameters. See table 1 for corresponding values for the aneurysm geometry.

<table>
<thead>
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<th>parameters</th>
<th>values</th>
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</thead>
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<tr>
<td>dynamic viscosity, $\nu$</td>
<td>$1.7 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$</td>
</tr>
<tr>
<td>haematocrit, $H$</td>
<td>42%</td>
</tr>
<tr>
<td>$N_{\text{RBC}}$</td>
<td>850#</td>
</tr>
<tr>
<td>$N_{\text{plt}}$</td>
<td>45#</td>
</tr>
<tr>
<td>diameter, $d$ (main vessel)</td>
<td>100 $\mu$m</td>
</tr>
<tr>
<td>length, $L$ (main vessel)</td>
<td>600 $\mu$m</td>
</tr>
<tr>
<td>spatial resolution, $\Delta x$</td>
<td>$1 \mu$m</td>
</tr>
<tr>
<td>time step, $\Delta t$</td>
<td>$9.8 \times 10^{-8} \text{ s}$</td>
</tr>
<tr>
<td>$C_{\text{plt}}$</td>
<td>$2.6 \times 10^{-3} \text{ plt} \text{ m}^{-2}$</td>
</tr>
</tbody>
</table>

\#Channel simulations.

Two cross sections are examined more closely for each of these cases, (a) corresponding to the main vessel flow and (b) for the others, and detailed profiles can be seen in figures 5 and 6.

The lateral position of platelets is visible for LLa010A and Sa010A in figures 6a and 5a, respectively. Both cases have a noticeably lower peak in the platelet concentration, closer to the neck of the aneurysm. This may yield an influx of...
platelets into the aneurysm, but no significant increase in the aneurysm concentration is evident (figures 7(iii), 6b and 5b), possibly due to the slow transport resulting from low velocities and small shear rates.

The initial distribution of platelets can be seen in the stagnation zones of figure 7, as an effect of their slow movement compared with the simulated time (figures 7(iii),(iv) and 6a).

### 3.4 Higher velocities

The Reynolds number for these two cases is $Re \approx 100$ and corresponds to a parent vessel velocity of $u_{\text{max}} \approx 1 \text{ m s}^{-1}$.

Lower velocities are found inside the aneurysm cavity (figure 8).

Three zones can be distinguished in the haematocrit and platelet distributions in the cases Sa100 shown in figure 9(i),(iii): (i) the main vessel flow, (ii) a region with high RBC density, and (iii) a recirculation zone in the centre of the aneurysm. Three zones are noticeable for LLa100 as well: (i) the main vessel flow with a part entering the aneurysm, (ii) a region with slightly higher haematocrit, and (iii) a recirculation zone. For each of the three zones, one cross section is examined more closely, (a), (b) and (c), respectively.
The lateral motion of platelets is present in the parent vessels of LLa100 and Sa100 as well. The concentrations are similar to those of the straight channel flow (figures 10a and 11a), but a considerably lower concentration of platelets is observed on the right-hand side of the wall, the side of the aneurysm orifice. Platelets flowing close to the wall are transported into the cavity and, owing to the periodic boundaries, the number of platelets is decreased in the channel.

This can be confirmed by the increased platelet concentration inside the cavity (figures 10b,c and 11b,c), providing evidence for an influx of platelets into the aneurysm, mainly increasing the outer parts of the recirculation zones.

A large area of high haematocrit is present in zone Sa100 (b), shown in figures 9 and 10b. The transport of RBCs there has formed a CFL on the top of the aneurysm, close to zone Sa100 (c). Platelets from the homogeneous initialization are trapped between RBCs in region Sa100 (b) and are visible as the steep peaks in figure 10b. A snapshot of this interesting situation is depicted in figure 1.

Comparing LLa100 with Sa100, a different behaviour is visible. A much smaller area with slightly more elevated haematocrit can be distinguished in LLa100 (ii) (figure 11b), but not to the same extent as Sa100 (b). A narrow CFL is also observed on the top, exhibiting an excess of platelets in contrast to the empty Sa100 (b) CFL. The higher concentration is depicted as a thin red layer following the boundaries of the aneurysm in figures 9 and 11b. Platelets most probably originate from the main flow and are transported there via the recirculation zone.

4. Discussion

In the current work, we studied the transport of platelets and RBCs in fast and slow flows, in two aneurysmal geometries with different aspect ratios. The distributions of cells inside the cavity are far from trivial.

Platelets flow closer to the vessel walls, remaining this way close to flow boundaries, e.g. walls or separation zones, where their function is beneficial. The connection of the platelet-rich CFL with the outer regions of the recirculation zones in the simulated fast flows enhances the transport of platelets inside the aneurysm and leads to an increased platelet concentration.

In the regions of high platelet concentration close to the top of the anurysmal wall, platelets may tether and roll, but the presence of activated platelets is also plausible, owing to a prior exposure to the higher shear rates in the orifice of the aneurysm. In the case of an unhealthy endothelium inducing coagulation, a thrombus could be formed in that region.

Another striking result of our simulations, however, is a large area of high haematocrit in the narrow necked case,
which can have a series of consequences. RBCs release ADP and thromboxane A2, which enhance the aggregation of platelets [51]. This can increase the levels of these agonists inside the aneurysm, promoting the activation of platelets and resulting in the formation of a thrombus. Moreover, the proximity of the RBCs to the endothelium does not constitute a physiological condition. The endothelium plays a significant role in the regulation of thrombosis [52] and, normally, RBCs are kept away from the wall via the CFL. This unhealthy situation can cause the release of procoagulants into the flow, resulting in the onset of a thrombus. Another aspect that should be noted is that the adhesion of RBCs to the endothelium has been linked to several vascular disorders [53], and such close vicinity of RBCs to the endothelium may contribute to the wall weakening and lead to a possible rupture of the aneurysm.

The pulsatility of the flow was neglected owing to the short time of the simulation (≈0.2 s) and, instead, two cases with high and low velocities were simulated. Low parent vessel velocities resulted in a stagnation zone inside the cavity, leaving the initial distribution almost unchanged. From this, we can argue that the fast flows within a cardiac cycle are those that determine the distribution of cells inside the aneurysm. The flow, however, traverses a spectrum of velocities and this estimation needs to be confirmed with more detailed studies.

To our knowledge, this is the first study exploring the transport of platelets and RBCs in aneurysmal geometries using explicit simulations of RBCs and platelets. The aneurysmal geometries used in the present work are 10 times smaller than normal aneurysms and more detailed studies are necessary in order to assess the importance of the current results to larger vessels. Nevertheless, the current work suggests that non-trivial distributions of RBCs and platelets are possible inside aneurysmal geometries and may contribute significantly to the formation of a thrombus inside the cavity.

‘Platelets’ in this study act like the latex beads used in in vitro experiments. Real platelets have a composite reactive behaviour, adhering to endothelial cells, aggregating with other platelets and rolling and tethering along the endothelial wall [54]. The authors are currently investigating modelling approaches and, in combination with in vitro experiments, will attempt to formulate a reliable micro-model for thrombosis and realize it in three dimensions.
Figure 10. Haematocrit and normalized platelet concentration for the cross sections of Sa100, as marked in figure 8(i). Shown here are cross sections from (a) the parent vessel, with the lateral position of platelets clearly visible. A lower concentration in the left side may be due to an influx into the aneurysm. (b) The increased haematocrit region. (c) The recirculation zone and its increased platelet concentration in the outer regions. The green line refers to the mean platelet concentration.

Figure 11. Similar to figure 10 but now for the LLa100 cross sections marked in figure 8(ii). Shown here are (a) margination behaviour of the parent vessel as in figure 10a; (b) and (c) exhibit an increased platelet concentration in the recirculation zone and a peak close to the walls where the RBCs are depleted.
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