A minimal model for metabolism-dependent chemotaxis in *Rhodobacter sphaeroides*

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Chemotaxis is vital cellular movement in response to environmental chemicals. Unlike the canonical chemotactic pathway in *Escherichia coli*, *Rhodobacter sphaeroides* has both transmembrane and cytoplasmic sensory clusters, with the latter possibly interacting with essential components in the electron transport system. However, the effect of the cytoplasmic sensor and the mechanism of signal integration from both sensory clusters remain unclear. Based on a minimal model of the chemotaxis pathway in this species, we show that signal integration at the motor level produces realistic chemotactic behaviour in line with experimental observations. Our model also suggests that the core pathway of *R. sphaeroides*, at least its ancestor, may represent a metabolism-dependent selective stopping strategy, which alone can steer cells to favourable environments. Our results not only clarify the potential roles of the two sensory clusters but also put in question the current definitions of attractants and repellents.

1. Introduction

Chemotaxis is biased random walk in gradients of beneficial or toxic chemicals, until relevant concentrations are optimal. In bacteria, chemotactic behaviour requires flagellar rotation and two-component signal transduction systems that comprises histidine kinases and response regulators. Unlike the well-known example of chemotaxis in *Escherichia coli*, some bacteria including *Rhodobacter sphaeroides* and *Bacillus subtilis* have more complicated signalling systems composed of multiple homologues of *E. coli* chemotaxis proteins [1–3].

Although it is widely believed that metabolism does not feedback to chemotactic behaviour, recent research challenges this prevailing concept of metabolism-independent chemotaxis by raising the issue that chemotaxis is constantly affected by the metabolic state. For instance, a number of chemotaxis proteins in *R. sphaeroides* may be involved in intracellular metabolic sensing [4,5], thus referring to this motility as metabolism-dependent chemotaxis. In this paper, we aim to gain insights into metabolism-dependent chemotaxis, specifically in *R. sphaeroides*, by mathematically modelling its minimal signal transduction pathway.

1.1. Metabolism-independent chemotaxis

The chemotaxis signalling pathway of *E. coli* is best-understood and considered largely independent of metabolism where cells only sense external attractants and repellents with membrane-bound receptor clusters [6,7]. As depicted in figure 1a, upon ligand binding to the membrane-bound chemoreceptors, histidine kinase CheA autophosphorylates and transfers phospho groups to its cognate response regulator CheY, allowing phosphorylated CheY (CheY-P) to interact with the flagellar motor switch complex, resulting in clockwise rotation of flagella and tumbling motion of cell. Without a chemical stimulus, CheZ rapidly dephosphorylates CheY, and flagella switch to default counter-clockwise rotation, causing the cell to run. Enzymes CheR and CheB enable recovery of the receptor activity to its pre-stimulus level by methylation and demethylation of the receptors, respectively [9,10]. Hence, the chemoreceptors are known as methyl-accepting chemotaxis proteins (MCPs). Meanwhile, CheW is required in chemotactic signalling transduction, as it links chemoreceptors and CheA [11].
In *E. coli* and some other species, dedicated receptors for oxygen, various sugars and some amino acids have been identified [12–14]. Chemotaxis towards ligand analogues supports the proposition that attractant sensing is only through the transmembrane chemoreceptors. Similarly, repellents like some weak acids may be sensed through these MCPs at different binding sites [15,16]. For instance, acids are also sensed in the cytosolic linker region of Tsr and Tar receptors at the end of the HAMP domain [17].

Although chemotaxis to some attractants supports metabolism by leading cells to nutrients, bacterial movement is not affected by the metabolic state in the cell, due to lack of signal feedback loops from metabolism pathways to the chemotaxis proteins. This insensitivity to metabolic states allows bacteria to navigate to the maximum concentration of attractants.

### 1.2. Metabolism-dependent chemotaxis

In contrast to the widely accepted concept of metabolism-independent chemotaxis, evidence for metabolism-dependent chemotaxis is raised in many species such as *R. sphaeroides, Azospirillum brasilense* and *Helicobacter pylori* [18–20]. In these bacteria, the metabolic state has an on-going effect on chemotaxis, with evidence including:

- chemotaxis to some attractants requires partial metabolism of these attractants [21,22];
- the role of a chemical can switch between attractant and repellent, depending on growth conditions and the chemical concentration [8,23];
- inhibiting the metabolic pathway of one attractant abolishes chemotaxis to this attractant, while bacteria still have chemotactic behaviour towards other attractants [22,24]; and
- inhibitors of metabolic pathways can act as repellents [18].

### 1.3. Chemotaxis pathway in *Rhodobacter sphaeroides*

*Rhodobacter sphaeroides* is a purple non-sulfur bacterium that can use a wide variety of energy sources depending on the availability in the environment. Its notably versatile metabolism stresses the essentiality of metabolic state to continuously affect chemotaxis. In fact, sensing of cellular metabolic state in this bacterium can be accomplished by an additional
cytoplasmic sensory cluster, which is absent in metabolism-independent chemotactic bacteria [25]. This cytoplasmic cluster is thought to cooperate with the transmembrane chemosensory cluster and together determine the response of the single unidirectional flagellar rotation, i.e. rotating or stopping [26,27]. The resulting response of the cell is either a run or a stop. During the stops, the bacteria presumably randomly reorientate through Brownian motion [28], resembling a tumble in E. coli.

Another important characteristic of *R. sphaeroides* chemotaxis is the presence of two types of flagella composed of different proteins Fla1 and Fla2 controlled by different chemotaxis proteins [4,26,29], but only Fla1 is exclusively expressed in wild-type cells in the laboratory [30]. Phylogenetic studies indicate that Fla2-mediated chemotaxis might be evidence for an ancient chemotaxis pathway [30]. Therefore, we focus on Fla1-mediated chemotaxis in this paper.

Fla1-mediated chemotaxis involves both transmembrane and cytoplasmic sensory clusters (figure 1b) [8]. CheW2, CheW1, and CheW4 in these clusters are responsible for controlling the CheA3s with dedicated MCPs and fine-tuning chemoreceptor sensitivity by accepting or donating methyl groups [31]. Upon binding of external attractants to the transmembrane chemoreceptors, CheA2 autophosphorylates and passes the phospho group onto response regulators CheY, CheY, CheY, CheB1 and CheB2 [32]. However, binding affinities of chemoeffectors at the transmembrane receptors have not been measured.

Although the cytoplasmic cluster is believed to sense the metabolic state, specific ligands have not been experimentally established [8], except for some dicarboxylic acids such as succinate and propionate, which are sensed by TlpT [33]. It is possible that molecules involved in respiration, especially succinate and propionate, which are sensed by TlpT [33]. It is possible that molecules involved in respiration, especially.

2. Material and methods

2.1. Chemotaxis pathway

The transmembrane and cytoplasmic sensory clusters are regarded as a metabolism-independent and a metabolism-dependent pathway, respectively. The former pathway only responds to extracellular ligand, whereas the latter senses the metabolic state, reflected by the amount of ATP. Minimal models for both pathways are constructed using ordinary differential equations, considering only the essential components involved, with details explained in the following paragraphs.

2.1.1. Metabolism-independent pathway

The essential structure of this pathway consists of transmembrane receptors, histidine kinase CheA3, response regulators CheY3, CheY4 and CheY6 and motor, as shown in figure 2a. We regard CheY3 and CheY4 as one molecule CheY3,4 for simplicity, as they are functionally redundant [34]. The associated rate constants are demonstrated in table 1.

The Ising-lattice model [38] and Monod–Wyman–Changeux [39,40] models suggest that receptors in clusters act cooperatively by allosterically activating or deactivating neighbouring receptor proteins. Here, we use the simplified Hill equation

$$A_2 = \frac{L_{in}}{K_1 + L_{in}}$$

(2.1)

with $K_1$ being the ligand-binding rate constant, $L_{in}$ the external attractant concentration and $n$, a Hill coefficient. This implies that external attractant binding increasing phosphorylation of CheA3. This is in contrast to observations in *R. sphaeroides* [41], but is meant to reflect an ancient selectivity stopping strategy [36] (see ‘Discussion’ section). The activated CheA3 phosphorylates CheY3,4 while changes in total phosphorylated CheY3,4 concentration are also affected by the available unphosphorylated CheY3,4 whose concentration is normalized by the total CheY3,4 concentration. Hence, the changes in phosphorylated CheY3,4 (denoted as Y3,4) is calculated as

$$\frac{dY_{3,4}}{dt} = k_2 \cdot A_2 \cdot (1 - Y_{3,4}) - k_3 \cdot Y_{3,4},$$

(2.2)

with $k_2$ and $k_3$ being rate constants of phospho transfer and dephosphorylation, respectively. As a result of phosphorylated CheY3,4 binding to the flagellar motor, *R. sphaeroides* has a chance to stop flagellar rotation, with stopping probability

$$P_{stop} = \frac{Y_{3,4}}{Y_{3,4}^0 + K_4^4}.$$  

(2.3)

where $K_4$ is a threshold parameter and $Y_{3,4}^0$ a Hill coefficient.

To summarize, in our model, an increase in environmental ligand level results in more phosphorylated CheA3, an increased concentration of phosphorylated CheY3,4 and eventually a higher stopping probability. With the presumed high sensitivity, the metabolism-independent pathway encourages the cell to run towards the maximum concentration of ligand. Figure 3 shows the simulated chemotactic behaviours based only on the metabolism-independent pathway (for simulation details, see §2.3).

2.1.2. Metabolism-dependent pathway

In this model, we assume that the metabolic state is represented by the amount of ATP, as ATP is the most common and direct energy source in cells, and it is required for all phosphorylation reactions. For simplicity, histidine kinases CheA3 and CheA4 are not considered. Thus, the key components of the metabolism-dependent pathway include external and internal metabolite, ATP, CheY6 and the motor, as shown in figure 2b. The rate constants in this particular model are provided in table 2.

The internal metabolite concentration $M_i$ depends on the extracellular metabolite concentration $M_e$ as follows:

$$\frac{dM_i}{dt} = k_{11} \cdot (M_e - M_i) - k_{12} \cdot M_i,$$

(2.4)

with $k_{11}$ being the diffusion rate of metabolite across the membrane and $k_{12}$ the catabolic rate of the metabolite. When transported inside cells, metabolite is catabolized to produce ATP, or inhibits...
ATP production if present at high level. Meanwhile, ATP production can also be inhibited at the presence of a metabolic inhibitor $I$. Here, the inhibitor is assumed to accelerate the rate of ATP degradation, resulting in

$$\frac{d\text{ATP}}{dt} = \frac{k_5 \cdot M_i}{K_7 + M_i} - k_6 \cdot \text{ATP} - k_8 \cdot I^{n_1} \cdot \text{ATP},$$

with $k_5$ being the ATP production rate; $k_6$, the ATP usage rate; $K_7$, the threshold parameter that allows saturation of ATP production; $k_8$, the inhibitory rate of metabolite; and $n_0$ and $n_1$ Hill coefficients.

Apart from supporting cellular activities, ATP is also used to indirectly phosphorylate CheY6, with the concentration of phosphorylated CheY6 given as

$$\frac{dY_6}{dt} = \frac{k_9}{C_1} \frac{\text{ATP}}{C_0} - \frac{1}{C_0} \frac{k_{10}}{C_1} \text{Y}_6,$$

with $k_9$ and $k_{10}$ the phosphorylation and dephosphorylation rate constants, respectively. Finally, binding of phosphorylated CheY6 at motor contributes to cell stopping, with the stopping probability given as

$$P_{\text{stop}} = \frac{Y_6}{K_m + Y_6},$$

where $K_m$ is a threshold and $m_1$ a Hill coefficient.

In summary, an increase in external metabolite concentration leads to ATP production, contributing to more phosphorylated CheY6 and consequently, a higher stopping probability. Hence, this pathway allows migration to places where optimal metabolism is achieved. Figure 4 shows the simulated chemotactic behaviours based only on the metabolism-dependent pathway.

As kinetic studies of the biochemical reactions are very limited, some rate constants were motivated by previous studies [37], while others were adjusted for convenience of the simulations to avoid saturation in the simulation box as adaptation was neglected.

### Table 1. Parameters of the R. sphaeroides metabolism-independent pathway. The asterisk marks that the parameter value is adapted from [37].

<table>
<thead>
<tr>
<th>parameter</th>
<th>value</th>
<th>unit</th>
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<tbody>
<tr>
<td>$K_1$</td>
<td>2.0</td>
<td>$\mu M$</td>
</tr>
<tr>
<td>$k_2$</td>
<td>0.6*</td>
<td>$s^{-1}$</td>
</tr>
<tr>
<td>$k_3$</td>
<td>0.3</td>
<td>$s^{-1}$</td>
</tr>
<tr>
<td>$K_4$</td>
<td>0.5</td>
<td>—</td>
</tr>
<tr>
<td>$n$</td>
<td>2</td>
<td>—</td>
</tr>
<tr>
<td>$m_1$</td>
<td>8</td>
<td>—</td>
</tr>
</tbody>
</table>

Figure 2. Minimal model for R. sphaeroides (a) transmembrane and (b) cytosolic sensory clusters. Blue arrows indicate phosphotransfer. (a) In the transmembrane chemotaxis pathway model, CheA2 autophosphorylation is increased upon external ligand binding to transmembrane chemoreceptors (activated CheA2 is denoted as $A_2$). Receptor activity is also dependent on ligand-binding constant $K_1$. The amount of CheY3-P and CheY4-P ($Y_{3,4}$) is dependent on $K_2$, phosphorylation rate $k_2$ and dephosphorylation rate $k_3$. Binding of CheY3-P and CheY4-P stops flagellar rotation, influenced by motor dissociation constant $K_4$. (b) In the cytoplasmic chemotaxis pathway model, internal metabolite (M) transported from external environment (Me) with rate $k_{11}$ is taken up and $k_{12}$ catabolized, producing ATP with rate $k_5$. Subsequently, ATP is used for indirect phosphorylation of CheY6 (CheY6-P denoted as $Y_6$) with rate $k_9$. Other usages of ATP include anabolism with rate $k_6$. CheY6 can also be gradually dephosphorylated with rate $k_{10}$. Binding of CheY6-P to motor leads to an increased probability of flagellar stopping, depending on motor binding constant $K_4$. (Online version in colour.)
2.2. Signal integration

As *R. sphaeroides* has a run-or-stop motor, the sum of running and stopping probabilities from each cluster is one. Hence, the following equation is obtained

\[
\left( P_{3,4\text{stop}} + P_{3,4\text{run}} \right) / C_1 = 1. 
\]

(2.8)

Assuming that integration of signals from both sensory clusters occurs only at the flagellar motor, we propose a modified OR logic gate that integrates the probability resulting from each pathway, with the integrated stopping probability calculated as

\[
P_{\text{stop}} = P_{6\text{stop}} + \left( 1 - P_{6\text{stop}} \right) P_{3,4\text{stop}}. 
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Equation (2.9) is obtained by expansion and extraction of the factors containing stopping probabilities from equation (2.8).

2.3. Bacterial movement

Based on the Euler method, *R. sphaeroides* is simulated to move or stop, determined by the integrated stopping probability at each time step, i.e. each second in our simulations. Bacterial movement is implemented by comparing the integrated stopping probability, \( P_{\text{stop}} \), with a random number between 0 and 1. When stopped, the simulated bacteria randomly re-orientate around the two-dimensional space, mimicking *in vivo* behaviour [28]. In the running mode, bacteria orient in the same direction, \( \alpha \), as in the previous step and run 20 \( \mu \text{m} \) in the simulation box. The speed 20 \( \mu \text{m} \text{s}^{-1} \) was chosen based on experimental data of

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<table>
<thead>
<tr>
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</tr>
</thead>
<tbody>
<tr>
<td>( k_5 )</td>
<td>43.90</td>
<td>( \mu \text{M}^3 \text{s}^{-1} )</td>
</tr>
<tr>
<td>( k_6 )</td>
<td>1</td>
<td>( \text{s}^{-1} )</td>
</tr>
<tr>
<td>( K_7 )</td>
<td>3.8</td>
<td>( \mu \text{M} )</td>
</tr>
<tr>
<td>( k_8 )</td>
<td>0.5</td>
<td>(( \mu \text{M} \text{s}^{-1} ))</td>
</tr>
<tr>
<td>( k_9 )</td>
<td>0.6</td>
<td>(( \mu \text{M} \text{s}^{-1} ))</td>
</tr>
<tr>
<td>( k_{10} )</td>
<td>0.6</td>
<td>( \text{s}^{-1} )</td>
</tr>
<tr>
<td>( k_{11} )</td>
<td>0.5</td>
<td>( \text{s}^{-1} )</td>
</tr>
<tr>
<td>( k_{12} )</td>
<td>0.1</td>
<td>(( \mu \text{M} \text{s}^{-1} ))</td>
</tr>
<tr>
<td>( m_2 )</td>
<td>8</td>
<td>—</td>
</tr>
<tr>
<td>( n_0 )</td>
<td>3</td>
<td>—</td>
</tr>
<tr>
<td>( n_1 )</td>
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\[

\begin{align*}
\text{Table 2. Parameters of the } R. \text{sphaeroides } \text{metabolism-dependent pathway.} \\
\hline
\text{parameter} & \text{value} & \text{unit} \\
\hline
k_5 & 43.90 & \mu \text{M}^3 \text{s}^{-1} \\
k_6 & 1 & \text{s}^{-1} \\
K_7 & 3.8 & \mu \text{M} \\
k_8 & 0.5 & (\mu \text{M} \text{s}^{-1}) \\
k_9 & 0.6 & (\mu \text{M} \text{s}^{-1}) \\
k_{10} & 0.6 & \text{s}^{-1} \\
k_{11} & 0.5 & \text{s}^{-1} \\
k_{12} & 0.1 & (\mu \text{M} \text{s}^{-1}) \\
m_2 & 8 & — \\
n_0 & 3 & — \\
n_1 & 2 & — \\
\hline
\end{align*}

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\text{Figure 3. Simulation of transmembrane cluster-mediated chemotaxis. (a) Trajectory of exemplar bacterium showing movement up the gradient from left to right in the simulation box. (b) Experienced local ligand concentration of simulated bacterium during 1000 s simulation period. (c) Stopping probability based only on the transmembrane sensory pathway. (d) The distribution of 50 independently bacteria along x-axis after 1000 s simulation time. (e) The final distribution of 50 simulated } \text{in silico} \text{ bacteria. Almost all the simulated bacteria migrate to the area where external ligand is abundant. (f) The external ligand concentration increases linearly in x-direction from } -500 \text{ to } 500 \mu \text{m. (Online version in colour.)}
Therefore, the displacements along the $x$- and $y$-axes are $x = 20 \cdot \cos (a)$ and $y = 20 \cdot \sin (a)$, in units of micrometres. All bacteria are simulated within a box of $50 \times 50 \ \mu \text{m}$. Meanwhile, reflecting boundary conditions are applied to prevent loss of bacteria within the box. To observe the collective chemotactic behaviour, 50 in silico bacteria are simulated independently with random starting points within the simulation box. The cellular signal levels are updated for each iteration to calculate the new stopping probability. Ultimately, the initial and final distributions of bacteria along the appropriate axes are compared in each simulation using the two-sample Kolmogorov–Smirnov (KS) statistical test.

3. Results

3.1. Simulation 1: chemotaxis towards a chemical sensed by both sensory clusters

This simulation is inspired by several experimental observations that chemotaxis to some chemicals requires transport and metabolism of these chemicals [21,43,44]. Here, we test *R. sphaeroides* chemotactic behaviours towards a transmembrane receptor ligand that can also be converted to ATP. The ligand concentration increases linearly from left to right in the simulation box.

As shown in figure 5, the stimulated bacterium tumbles around high attractant concentrations, as the integrated stopping probability, $P_{\text{stop}}$, levels off at around 0.9 after 200 s. This movement pattern also applies to the other *R. sphaeroides* bacteria, as all the bacteria started from random positions clearly accumulated around high concentrations. The KS test proves the significant difference between the final and the initial distribution ($p < 0.01$).

3.2. Simulation 2: a metabolite can switch from an attractant to a repellent at very high concentration

As observed in Simulation 1, many bacteria do not move to the maximum attractant concentration. Such behaviour is also documented in aerotaxis. In response to an oxygen concentration gradient, *R. sphaeroides* returns to medium concentrations, forming a band [45]. To explore the reason for this behaviour, we conduct another simulation in which we allow for an even larger concentration range. In this case, it is assumed that only cytoplasmic cluster can sense the...
metabolite, which is set up to sharply increase in concentration along the x-axis. Interestingly, as shown in figure 6, the bacterium immediately returns to the middle of the box once it faces extreme concentrations of metabolite. By contrast, tumble motion dominates in the middle of the box, as directed by a higher stopping probability that resulted from the cytoplasmic sensory pathway. The behavioural pattern along the x-axis explains how multiple bacteria form a band in the middle of the box. The KS test supports that the initial and eventual cell distribution along the x-axis significantly differ ($p < 0.01$). A minor number of cells are found in the very right end of the box where the attractant concentration is highest. These, however, are eventually also trapped in the middle of the box.

3.3. Simulation 3: chemotaxis towards two functionally different chemicals

Rhodobacter sphaeroides has been shown to perform chemotaxis towards two functionally similar chemicals [46]. Additionally, bacteria may also need to simultaneously sense and chemotaxis towards functionally different beneficial molecules such as enzyme cofactors and carbon sources, assuming differential functionality means that absorption of the chemical leads to direct alterations in energy production. For example, the transmembrane chemoreceptor ligand may not directly contribute to producing ATP, while cytoplasmic receptor TlpT can sense some dicarboxylic acids that are commonly used as carbon source [33]. However, previous modelling of chemotaxis at the molecular level has only used one concentration gradient at a time [47], and there is currently no published investigation about chemotaxis towards functionally different chemicals. Here, we test if the simulated cells can respond to gradients of two functionally different chemicals.

As shown in figure 7, bacteria favour the region where both attractants are relatively abundant, although they do not tend to explore maximal concentrations of both external ligand and metabolite. This is due to the saturation of both chemotaxis pathways, and corresponds to our other simulations that bacteria stop before reaching the highest concentration regions. Statistical analysis by the KS test
shows a change in cell distribution along both axes after 1000 s is significant ($x$-axis $p < 0.01$; $y$-axis $p < 0.01$).

### 3.4. Simulation 4: metabolic inhibitors can block chemotaxis towards the dedicated metabolite

Experiments have shown that inhibition and artificial mutation of key components in the metabolic pathway can abolish chemotaxis to that attractant. For example, methionine sulfoximine that inhibits ammonia assimilation can significantly interrupt chemotaxis to ammonia [43]. In addition, knocking out fructose metabolic pathway blocks chemotaxis towards fructose but not other attractants such as succinate [22]. Here, an inhibitor that blocks the metabolic pathway sensed by the cytoplasmic sensory cluster is evenly distributed (2 $\mu$M) across the simulation box. Ligand and metabolite concentrations are the same as in Simulation 3, with the results presented in figure 8.

The inhibitor can completely block the signalling at the cytoplasmic cluster. Based on the OR gate algorithm (eqn 2.11 in Methodology), the stopping probability, in this case, equals the stopping probability resulting from signalling by the transmembrane sensory cluster. Thereafter, the in silico bacteria show more running motion towards high ligand concentrations. According to the distribution of 50 simulated independent bacteria clearly exhibits accumulation in the middle of the box. (e) Corresponding endpoints of 50 trajectories. (f) The range of the metabolite concentration is twice as large as in the previous simulations in figure 5. (Online version in colour.)

### 3.5. Simulation 5: metabolic inhibitors can act as repellents

In other bacteria like *A. brasilense*, inhibitors including oxidized quinones that interrupt metabolic pathways actually act as repellents [18]. Similar experiments have not been conducted for *R. sphaeroides*. Thus, we would like to theoretically test whether an inhibitor can act as a repellent in this species. In this simulation, only the cytoplasmic sensory cluster is tested, as the inhibitor acting on the metabolic pathway...
The control for this experiment is the bacteria distribution in presence of a constant metabolite concentration and absence of inhibitor, as shown in figure 9. The results show that compared to the randomly distributed bacteria in the control group, bacteria facing the metabolism inhibitor favour areas with low inhibitor concentration. Also there is a statistically significant difference between the cell distribution in control and test groups ($p = 0.01$). This is because the inhibitor reduces synthesis of ATP, which leads to less phosphorylated CheY6, encouraging bacteria to swim away from the inhibitor. When bacteria are distant from the inhibitor, the stopping probability resulting from high cytoplasmic signalling level approaches 1, contributing to flagellar stopping.

4. Discussion

Bacterial chemotaxis has been traditionally studied independently from metabolism. However, recent genomic studies show that metabolism-dependent chemotaxis in species like *R. sphaeroides* may be achieved through metabolic sensing by the cytoplasmic chemoreceptors and possibly integration of signals from both transmembrane and cytoplasmic sensory pathways. Here, we have provided a novel mathematical modelling approach to the unsolved problem of cytoplasmic sensory pathway signalling and integration of both sensory cluster signals in *R. sphaeroides*. Based on the minimal model where only essential molecules are considered, the simulations agree with available qualitative data in literature. Quantitative data is not used to compare with simulation results due to their limited availability.

An advance of this model is the cooperation of metabolic sensing with classic metabolism-independent chemotaxis. Previously, it was suggested that the signal integration site in *R. sphaeroides* might be CheA2, as deletion of CheA2 removes tactic behaviour [25]. Our model proposes an OR gate for integration at the motor level, producing realistic bacterial behaviours while reducing the complexity of crosstalk between the different pathways. However, there are two shortcomings of our minimal model. First, we neglect adaptation of both receptor clusters to avoid additional
be interchangeable. Simulations 1 and 2 suggest that a

of how to define an attractant or a repellent, because they can

adaptation pathways, an AND gate also may work.

brane and cytoplasmic signalling pathways are interlinked by

chemotaxis to both an external attractant and a metabolite. Note that our minimal model
gellar motor, and thus could have implemented such

metabolite, when present at certain concentrations, can cause signal saturation and may even switch to a repellent, corresponding to the microaerophilic and microaerophobic behaviours observed in aerotaxis [45]. Precise definition of attractant and repellent may be more complicated as the role of a metabolite also depends on cell culture conditions [48,49], so that photosynthetically grown *R. sphaeroides* may regard oxygen as a repellent, as coexistence of light and oxygen can produce fatal reactive oxidative species.

In addition, there is experimental evidence that inhibition of metabolic pathways abolishes chemotaxis towards this metabolite. Based on the modelling (Simulation 4), we predict that the inhibitor can indeed act as a repellent for *R. sphaeroides*. In fact, experiments on other species like *A. brasilense*, whose chemotaxis mechanism also depends on metabolism, imply that cells avoid exposure to inhibitors of the ETS [18]. Hence, it is realistic to suggest that the role of a chemical may be defined through its effect on energy generation.

The results of several simulations stress the importance of the cytoplasmic sensory cluster, as it can nearly determine cell

cross-talk via uncharacterized reactions. A downside of this is that our model parameters require some fine-tuning. Second, we technically do not implement a run-and-tumble chemotaxis strategy, but a simpler selective stopping strategy. This potentially ancient strategy allows cells to simply swim until they find favourable conditions and then stop [36].

Precise definition of attractant and repellent may be more complicated as the role of a metabolite also depends on cell culture conditions [48,49], so that photosynthetically grown *R. sphaeroides* may regard oxygen as a repellent, as coexistence of light and oxygen can produce fatal reactive oxidative species.

In addition, there is experimental evidence that inhibition of metabolic pathways abolishes chemotaxis towards this metabolite. Based on the modelling (Simulation 4), we predict that the inhibitor can indeed act as a repellent for *R. sphaeroides*. In fact, experiments on other species like *A. brasilense*, whose chemotaxis mechanism also depends on metabolism, imply that cells avoid exposure to inhibitors of the ETS [18]. Hence, it is realistic to suggest that the role of a chemical may be defined through its effect on energy generation.

The results of several simulations stress the importance of the cytoplasmic sensory cluster, as it can nearly determine cell
movement by itself (Simulations 1, 3 and 5). There are several observations that support this idea. Firstly, sensitivity of the cytoplasmic sensory cluster can be increased by splitting a kinase into an ATP binding protein (CheA4) and a phosphatase (CheA3), and joining them together as a heterodimer [50]. Secondly, experimental observations have indicated the ability of CheY6 to stop the flagellar motor alone, probably due to multiple phosphorylation sites [34]. Finally, some attractants like fumarate may not be sensed through the transmembrane sensory cluster at all. Instead, fumarate acts on flagellar rotation via a respiratory protein fumarate reductase [51], which can potentially be sensed by the cytoplasmic sensory cluster.

As simulated cells mimic chemotaxis observed in wild-type R. sphaeroides, even when the transmembrane sensory pathway is not considered (Simulation 2), one might wonder why a transmembrane sensory cluster is necessary at all? As R. sphaeroides shows strong chemotaxis towards many different sugars, it may be unrealistic to possess different chemoreceptors for each specific ligand in the membrane [22]. This evidence suggests that carbohydrates may not be sensed through the classic transmembrane MCP pathway. However, other experiments indicate that both sensory pathways must work together to support chemotactic behaviours [34,52]. Some researchers believe having many CheY proteins may allow the molecules to compete for binding, even without actually stopping the flagellar rotation [53]. Therefore, upon external ligands binding to receptors, phosphorylated CheY5 and CheY6 may only compete with phosphorylated CheY3 for binding to the flagellar motor switch complex, without stopping flagellar rotation themselves. Of course, sensing toxins by transmembrane receptors avoids having to take them up prior to sensing. Further biochemical research is necessary to identify the ligands of transmembrane chemoreceptors, as well as the roles of different chemotaxis proteins.

Our simulation results suggest that ATP may play a key role in chemotaxis signalling. Indeed, ATP is both an essential reactant for phosphorylation of the chemotaxis proteins and a product of energy generation. Its ability to change rapidly in R. sphaeroides provides the potential to affect chemotaxis significantly [54]. Note, however, that our minimal model of metabolism-based chemotaxis does not model sensing of the metabolites by the cytoplasmic cluster explicitly. This

**Figure 9.** Simulation 5: metabolic inhibitors can act as repellents. In this simulation, the metabolite is evenly distributed in the simulation box (figure not shown). (a) Exemplar trajectory showing that bacterium runs away from high inhibitor concentrations at the right in the simulation box, and that it stops at the left of the simulation box. (b) Within 1000 s simulation time, the bacterium in (a) avoids the inhibitor. (c) The signal from cytoplasmic sensory pathway increases significantly as the local inhibitor concentration drops. (d) The distribution of 50 simulated bacteria along the x-axis evidently indicating that most bacteria avoid the inhibitor. A few bacteria are observed at area where inhibitor concentration is high, but they will eventually join the others. (e) Trajectory endpoints of 50 in silico bacteria. (f) Linear inhibitor gradient in x-direction. (Online version in colour.)
reflects the idea that our model represents an ancient version of *R. sphaeroides* chemotaxis. Hence, to avoid large changes in intracellular ATP levels, which may be detrimental for many other aspects of cellular functioning, the cytoplasmic sensory cluster may have evolved to sense some metabolites directly, and not indirectly via ATP.

Current experimental data suggest that metabolism-dependent chemotaxis may be more complex than previously thought, owing to differential gene expression in different environments. For example, PrrB/PrrA two-component system up-regulates photosynthesis in *R. sphaeroides*, and the expression is stimulated by low oxygen conditions [55].

This implies that at very low concentration, oxygen may no longer be an attractant, but may cause bacteria to start phototaxis. The coupling between gene expression and tactic response can be very beneficial to cells by enhancing adaptation to their changing environment.

Unfortunately, using a more realistic model to simulate complex metabolism-dependent chemotaxis is still limited by the lack of quantitative experimental data and kinetic studies. For example, some reactions in the signalling pathways, the nature of the ligands of the cytoplasmic receptor cluster, the binding sites of the CheY proteins on the motor switch complex, the origin of signal integration, cross-talk and synchronization of the two of sensory pathways are yet unclear. A stronger collaboration between experimentalists and theoretical systems biologist is required to improve our understanding of metabolism-dependent chemotaxis.

Acknowledgements. We are thankful for helpful discussions with Judy Armitage. This work was initiated during S.F.'s final-year undergraduate project.

funding statement. R.E. thankfully acknowledges funding from the ERC Starting grant no. 280492-PPHIP.

References


21. del Campo AM, Ballard T, De la Mora J, Poggio S, Camarena L, Dreyfus G. 2007 Chemotactic control of the two flagellar systems of *Rhodobacter sphaeroides* is mediated by different sets of CheY.