Schools of fish and flocks of birds: their shape and internal structure by self-organization

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Models of self-organization have proved useful in revealing what processes may underlie characteristics of swarms. In this study, we review model-based explanations for aspects of the shape and internal structure of groups of fish and of birds travelling undisturbed (without predator threat). Our models attribute specific collective traits to locomotory properties. Fish slow down to avoid collisions and swim at a constant depth, whereas birds fly at low variability of speed and lose altitude during turning. In both the models of fish and birds, the ‘bearing angle’ to the nearest neighbour emerges as a side-effect of the ‘blind angle’ behind individuals and when group size becomes larger, temporary subgroups may increase the complexity of group shape and internal structure. We discuss evidence for model-based predictions and provide a list of new predictions to be tested empirically.

Keywords: self-organization; shape of a group; flock of birds and school of fish; internal structure; locomotion; collective motion

1. INTRODUCTION

Models of self-organized systems have more and more proved to be helpful in explaining the behaviour of groups of animals; we refer to insects [1,2], fish [3,4], birds [5], primates [6,7] and humans [8]. Most importantly, these models develop an integrative picture of the connection between traits at the level of the individual and of the group. For instance, in a model of collective movement, the increase in density in a swarm results in a phase transition from an unaligned swarm to an aligned school. A similar phenomenon is found in swarms of locusts [9,10].

In the present review, we show how these models have contributed to our understanding of the shape and the internal structure of travelling groups of fish and of birds. We confine ourselves to the situation in which predators are absent. The effect of predators on the shape of groups is enormous and deserves a separate review. We show the kinds of insights and predictions we may gain through models with a high potential for self-organization. Here, starting from local interactions, it is shown how patterns at a higher level develop by self-organization. We test some of the model-based predictions against empirical evidence and list others to be tested empirically in future. We limit ourselves to models of self-organization that are based on biologically inspired rules regarding movement behaviour. Explanations generated in this way are usually new, and have not been thought of without the help of these models. With this method, we show that group shape, internal structure or both are strongly influenced by a number of traits: (i) the specifics of locomotion (swimming or flying), (ii) the locality of interaction, (iii) the heterogeneity of the environment and (iv) the field of perception. Besides, we treat a model that represents not only schooling, but also its hydrodynamics and is used at present for studying energetic advantages of schooling.

We discuss models of moving schools and flocks that are individual-based and spatially explicit. In these models, individuals are moving, while they are attracted to others, align with them and avoid collisions [11–15]. There is a variety of models of fish schools that may differ in details. For the present survey, it is important whether individuals adjust their speed or not [11,15], and the number of neighbours to which they adjust their velocity [5,14–17]. Models dealing with birds [18,19] do not usually differ substantially from models of fish [13,20] apart from one exception, the model StarDisplay. In it, the behavioural rules of coordination (attraction, alignment and avoidance) are extended with a number of characteristics of birds [5,15]: modelled individuals fly instead of swim. They follow simplified (fixed-wing) aerodynamics, i.e. they experience lift, drag and gravity [21]. In order to fly along a curve, individuals avoid slipping by rolling into the direction of the turn. They thus reach a certain angle to the horizontal plane, the so-called banking angle,
such as real birds do [22]. Flocks in our model StarDisplay are sometimes made to remain above a sleeping site such as starlings at dawn above their sleeping site in Rome [23, 24]. Computer models of energy saving in schools of fish must include the hydrodynamics of swimming by fish [25].

We examine the shape of schools and flocks with measures similar to those used in empirical studies.

1.1. The basic models in two dimensions and in three dimensions

Individuals in these models of fish schools and bird flocks have a position in two-dimensional space or in three-dimensional space. They move at a certain speed. Speed is either adjustable, slowing down to avoid collisions and speeding up to move towards others [15], or stochastically variable around a certain average value [11, 14]. The new velocity of an individual depends on its interaction partners, also referred to as influential neighbours (figure 1). Influential neighbours have been chosen in several ways, e.g. neighbours are chosen depending on their proximity to the actor [11], their proximity plus a fixed number, also called topological range [11, 23], or their visibility to the actor [16]. The position and heading of these influential neighbours determine the new velocity of each individual. Apart from random noise, the new velocity depends on the weighted sum of being attracted to influential neighbours, aligning with them and avoiding them.

Even in those fish models in which the location is given in three dimensions, the direction of movement is still mostly in the horizontal, because the individuals almost exclusively perform yaw (figure 2), because in fish models other movements (pitch and roll) are largely prevented [13, 15, 26]. In the bird model StarDisplay, however, individuals move in all directions. The individual’s flying behaviour is represented by fixed-wing aerodynamics based on thrust, drag, lift and gravity. The individuals in the model are...
2. RESULTS

2.1. Fish schools: shape and density distribution

The main function of schooling and flocking is considered to be a reduction in the risk of predation [30]. Therefore, it has been suggested that the optimal shape of a school of fish should be spherical, because this combines the smallest surface for any volume and so the school would run the smallest risk of being discovered by a predator [31–36]. In reality, however, school shape is hardly ever spherical [37], but usually oblong [31,38–43]. Note that here shape is considered as being seen from above in two dimensions. The oblong shape is believed to protect against predation by ambush predators, because it reduces the size of the frontal area, where these predators are supposed to attack [44]. The stability of the shape of fish schools is remarkably greater than that of bird flocks. The shape of flocks of birds varies both in a single flock and between different flocks [45].

What causes the shape of schools of fish to be oblong has been investigated with the help of individual-based models of self-organized schooling. In these models, individuals have a tendency to move and to follow rules of attraction to others, alignment with them and avoidance of collisions [14,15,28,46]. In these models, the emergence of the oblong shape is robust (see the electronic supplementary material, movie S1): it is found for most school sizes, unless schools are very large [15,28,46], for schools of high and low cruise speed (figure 3a) [46], for schools that are free-swimming and travelling in a tank [28] and for schools with mixtures of different percentages of large and small individuals [46] even if these individuals of different body sizes are attracted to others of similar size [46].

The oblong shape emerges in the model because, during travelling, individuals must sometimes slow down to avoid collisions. They slow down (rather than speed up) because they perceive more easily someone too close in front of them than behind them, represented by their so-called blind angle backwards (figure 1c). By slowing down to avoid collision, an individual (here in black, figure 3b) [28] leaves a gap between its former neighbours and subsequently these former neighbours move inwards closer together (time 2 in figure 3b). Thus, the school becomes oblong and lengthens until no further avoidance is needed. At this point, a temporary equilibrium is reached (time 3, figure 3b). Even when turning, the shape of a school remains oblong in the model (figure 4a). This is due to the fact that individuals adjust their velocity according to the proximity of others. When moving in the inside of an angle, they come so close together that they slow down automatically, whereas on the other hand when they move in the periphery they move further apart, so that they have to speed up. In this way, the shape of the school is preserved.

In the model, decelerating also affects the internal structure of the school in such a way that the density becomes highest at the front. This happens because slowing down builds up and lengthens the tail of the school, which is automatically less dense than the front (figure 5a,b).

Support for our model-based theory of the causation of the oblong shape comes from three sources, namely simulation experiments, existing empirical data and...
empirical tests of our model-based predictions [28]. In the models, larger schools tend to be relatively more oblong and denser. This holds in models in two dimensions and three dimensions both when schools move in infinite space (figure 3a) and in a tank (figure 3c) [14,28,46]. Large schools are more oblong in these models owing to a shorter distance to the nearest neighbours, because this forces individuals to avoid collisions more often (figure 3a,b). The greater density of larger schools in turn is a consequence of the greater attraction among the larger number of individuals, especially of the peripheral individuals inwards, which can be seen as a ‘surface pressure’.

In our model, faster schools prove to be less oblong (figure 3a) [15]. This is due to greater inertia of the individuals, which makes them wiggle less. Consequently, the path of the school is straighter (figure 6a–c) and school members are more aligned (figure 6d), as has been shown in other models also [15,48,49]. Therefore, individuals have to avoid others less often and fall back less frequently. By the same processes, via the higher frequency of avoidance [15], a larger tail builds up when schools are larger in our model and when the speed is slower (figure 5a), causing the highest density to be more frontal (figure 5b). If the speed is slow, the inertia is lower. This leads to weaker alignment and a more tortuous trajectory of the centre of gravity of the school (figure 6). Consequently, the densest kernel in the front of the school becomes less dense and the tail is denser than if speed is higher (figure 5a).

In line with our models, existing empirical data show the following patterns: density is highest at the front [44], larger schools of many species of fish are denser [28,41,50–54], larger schools of saithe (Pollachius virens) are more oblong [41] and slower schools of saithe and cod are more oblong than faster ones [41]. Besides, our experimental setup with schools of 10–60 mullets confirms that larger schools are both denser and more oblong (figures 3c and 5c) [28]. Further, the crucial observation in the model that fish in a school slow down to avoid collisions and speed up to keep up with others is confirmed in empirical data of golden shiners and mosquitofish [55,56].

In large schools of very many individuals, shape is not oblong and internal structure is complex. For instance, the shape of schools of tens of thousands of anchovies, herring, sprat or saithe comprises pseudopodia and inwards bends, and their internal structure shows kernels of high density and vacuoles of low density. This complexity is supposed to result from partially independent movements of micro-groups or sub-schools [57,58]. In line with this, in a model of schools of tens of thousands of fish, a complex shape with pseudopodia and a heterogeneous internal structure with vacuoles emerges (figure 5d). This happens when individuals interact more locally (i.e. with a lower percentage of the school members) than is usual in these models [16]. For instance, in the model by Kunz & Hemelrijk [16], locality of interactions arises from the limited perception range of individuals (figure 1c): they perceive only those who are not hidden behind neighbours closer by [16]. Note that this is a more natural representation of influential neighbours than that in the usual approach in which either all individuals in a metric range are included [11–13], even if this range is shortened during...
crowding [15], or a fixed number of nearest neighbours, i.e. topological range, is concerned [5,11,47].

2.2. Bird flocks: shape and distribution of density

The shape of flocks of birds is only rarely oblong: it differs between flocks and, in one and the same flock, it varies over time [45]. For instance, when a flock of rock doves or starlings is turning, the empirical data of the three-dimensional positions of its members show that density temporally increases and decreases, and the orientation of the flock changes relative to the direction of movement [59,60]. Besides, it has been observed in pewits, dunlins and starlings that individuals swap positions [23,45,60,61]. The same is found in our model, StarDisplay (see the electronic supplementary material, movie S2) [47]. In this model, the variability of shape, density and individual positions is a consequence of the constraints of the flying behaviour and of the locality of interaction.

Constraints of flying behaviour contain the rolling behaviour during turning and the low variability of the speed. First, during turning, individuals of the model have to roll into the turn to generate sufficient centripetal force for turning and for avoiding slipping out of the turn. Consequently, in the model, individuals lose effective lift (figure 2b). This results in a loss of altitude (figure 4b). Therefore, during such turns, the shape of the flock is variable also in the vertical direction. Similarly, also real birds lose altitude during turning, e.g. rock doves and steppe eagles [59,62]. Second, owing to (energetic) constraints of flying, individuals hardly slow down [63]. Therefore, during a turn, all individuals of a small flock follow a path of equal length and curvature (figure 4c). As a consequence, they change direction relative to the shape of the flock and therefore the shape of the flock changes in relation to the direction of movement. For instance, when the flock shape in the movement direction is oblong and all flock members turn 90° to the right (figure 4c), after the turn it will be wide in the movement direction. This turn is accompanied by swapping of locations between individuals: for instance, individuals located at the front before turning are located at the right side after turning [47]. Furthermore, the low variability of speed causes the distance to the nearest neighbours to be similar in the front half and the back half of the flock, as in large flocks of starlings [60].
Similarly, in the fish model, if we make individuals swim at almost fixed speed, individuals swap positions during turns, school shape changes relative to the direction of movement and the density is similar at the back and front (figure 4d) [47].

As to the effect of locality of interaction on variability of flock shape, we consider three causes. First, heterogeneity of environment: in StarDisplay, the environment consists of a ‘preferred space’ above the sleeping site and the space outside it. This preference causes temporary compression of large flocks, when some individuals have moved outside the preferred space, whereas others still fly in it. Consequently, individuals of a single flock may turn at different times in order to return to the preferred space. If the frontal individuals already have turned, but those in the rear still move outwards, the frontal individuals will approach those at the rear; thus, the flock compresses. Indeed, such a temporal increase in density during turning has been recorded in real flocks also [59].

Second, large flock size: even when flying approximately in a straight line in a homogeneous environment, larger flocks generate larger sub-flocks that move more independently and this will increase variability of flock shape [47]. In the model of starling flocks, StarDisplay, this arises because the velocity of individuals has been shown to be correlated to that of others close by. The correlation length (which reflects the temporary size of the sub-flock) appears to increase linearly with size of a flock with a slope of 0.44 (figure 7a) [47]. A similar correlation is found in empirical data of flocks of starlings [64], but the slope is steeper in the model than in empirical data (0.44 in the model versus 0.35 empirically). This is probably a consequence of the lower ‘disturbance’ in the model owing to its lack of factors such as wind and predators. When modelled flocks are larger, ‘sub-flocks’ appear to become also more diverse in their movement direction. This is apparent because the polarization in the whole group decreases with group size, whereas local polarization, as
measured among nearest neighbours, remains constant independent of group size (figure 7b) [47].

Third, a low number of interaction partners: when interactions are more local, subgroups move more independently and therefore the flock shape will become more variable. This arises because the lower the number of interaction partners is, the smaller is the size of the sub-flocks and the weaker is the slope of the correlation between flock size and size of sub-flocks, as can be seen by comparing the regression line for 6.5 interaction neighbours (solid line in figure 7a) and 50 interaction neighbours (dashed line in figure 7a) [47]. Besides, with a high number of interaction partners, flocks are denser and the shape is more static and closer to a ball shape [47].

The composition of these sub-flocks changes with time in the model (see the electronic supplementary material, movie S3). When interactions are more local (i.e. when the flock size is larger, the number of interaction partners is lower, or both), such fluctuations of velocity are slower and larger [65]. This holds even when the distance to the nearest neighbour is kept the same for the different numbers of interaction partners.

2.3. The angle to the nearest neighbour, the ‘bearing angle’

The distribution in the group of the angle between the movement direction of an individual and the direction to its closest neighbour has been studied in schools of fish and in flocks of birds. This angle is called the ‘bearing angle’ (figure 8a) [36,66], but the ‘bearing angle’ is also used to refer to the most frequent angle to the closest neighbour in the whole group (figure 8b,c). This angle was considered to be adapted to two functions in a travelling group, namely to optimal vision through the school to detect a potential predator [67] or monitor each other [41], and to the optimal angle to exploit the

Figure 8. Bearing angles. (a) Bearing angles $\theta$ or direction towards the nearest neighbour from the perspective of individual $V_1$ and of individual $V_2$. Bearing angle of $V_1$ points 135° forwards (or 45° backwards), of $V_2$ it points 45° forwards. (b) Distribution of directions of nearest neighbour (i.e. ‘bearing angles’) in StarDisplay [5,47]. Circles: average angular distribution of empirical data of flocks of starlings [60]. Rectangles: average angular distribution of modelled flocks of same size as empirical data without a blind angle for separation. Triangles: average angular distribution of modelled flocks of individuals with a blind angle of 90° at the back (or 45° from the midline). Grey dashed curve: averaged nearest neighbour distribution of 100 randomly chosen flocks in the model. Dashed line: expected value for a random isotropic system, where the probability to find any bearing angle is the same for all angles $P_{\text{random}}(\cos(\theta)) = \frac{1}{2}$. Standard error bars are smaller than the symbols. (c) Distribution of highest frequency of bearing angles in model of fish schools (indicated by vertical lines) [15] for different sizes of the full blind angle, namely of 120°, 130° and 140°. (d) The relationship between blind angle (halved) and bearing angle towards nearest neighbour (NN) ahead (vertical lines in (c)) in the model of fish schools. For blind angle, see figure 2a.
wake from others [41,68]. As to the hypothesis of optimal vision through the swarm, no specific bearing angle has been suggested. With regard to gaining energy from the wake of others, flocking birds were assumed to save energy by flying in V-formation, which indeed has been confirmed in empirical data [69]. Note that flying in the usual, less-ordered flock (cluster-flock) appeared costly in energy [70]. For schools of fish, a specific rigid formation, the so-called diamond-like structure, was predicted to reflect maximal energy saving [66]. Empirical data on bearing angles however showed that in schools of several species of fish the predicted rigid formation was not found [39,41,54,71]. Nevertheless, a number of facts indicate hydrodynamic benefits: for instance, individuals were shown to use less oxygen when in a school than when alone [67,72]; they beat their tail or fins slower at the rear of schools than elsewhere [73–76]. Also, they have been shown to exploit the wake behind a pillar [77,78]. In order to understand how fish save energy by moving in a school rather than alone, empirical studies should be supplemented with computer simulations, because it is empirically very difficult to measure forces of lift and drag particularly in a school and to measure what happens to the interacting wakes of several fish. Such a model should represent both the schooling of the individuals and the hydrodynamics. Recently, a particle-based simulation of schooling, using the so-called multiple particle collision dynamics (MPCD) method or stochastic rotation dynamics (SRD) method, has been applied: in it, hydrodynamics emerges from the interaction of 30 million particles among themselves and with the undulating fish [25,29]. In this simulation, the undulation of fish induces the same wake as in real fish, i.e. the reverse von Kármán street (figure 9) [25]. At present, we study in it the advantages of swimming in schools with different rigid spatial configurations, such as a diamond configuration [66] and others.

So far, it is thus unexplained what causes the specific bearing angles and their great variability observed in schools of fish and cluster-flocks of birds [79]. In cluster-flocks of birds, the bearing angle was found at 90° in starlings [60] and at 45° in dunlins [80]. In fish, the bearing angle was at 90° in cod, in herring at 45° and in dunlins to the dense flocking [80], that of 90° in cod to facultative schooling [41] and in starlings to the extremely sparse flocks [23,60]. Further, we may attribute the occurrence of both angles (45° (135°) in herrings to the obligatory schooling [41] and in dunlins to the dense flocking [80], that of 90° in cod to facultative schooling [41] and in starlings to the extremely sparse flocks [23,60].

3. DISCUSSION

In this study on collective motion of fish and birds, we have surveyed model-based explanations for the causation of group shape, group density and distribution of the bearing angle.

Model-based explanations have highlighted the importance of properties of locomotory behaviour and sensory perception. For instance, owing to swimming at a constant depth and slowing down to avoid collisions, the shape of schools is oblong. The larger vertical movements of flocks of birds due to their rolling during turning cause a shape that is variable in the vertical direction. Speed is more constant in our models of birds than of fish due to the constraints imposed by flying. This leads to more variation in the orientation of shape relative to its movement direction during turning in flocks of birds than in schools of fish. In the case where flocks move straight forward, the orientation of their shape depends on the initial orientation. Low variability of speed also leads to a more homogeneous distribution of density in the group than variable speed does, which explains the difference in density distribution between fish schools and bird flocks. Interactions that are more local (in the case of a lower number of interaction partners, a larger group, or both) result in a more complex shape and structure of groups of both fish and birds.

Figure 9. Wake behind a swimming mullet in MPCD or SRD model [25].
Sensory constraints represented by the limitation of the field of perception as a result of the blind angle determine the bearing angle in dense groups, in our models of both fish and birds. At present, we are studying in our models of hydrodynamics and schooling also the possible hydrodynamic advantages of schooling [25].

These model-based explanations are process-oriented, i.e. based on interactions among individuals and between individuals with their environment. For their invention, simulation experiments have been essential. They do not refute other explanations. In reality, shape and internal structure are likely to be influenced also by other factors, such as in fish by hypoxia, water temperature and depth [82,83] and in birds by air density and wind [84]. Such trade-offs are not discussed here because they have not yet been studied in models of self-organization.

Explanations generated by these models can be falsified empirically because they are based on several patterns that can be verified in empirical data.

Testable predictions concern, for instance, the following.

— If variability of speed is high:
  - shape is less oblong, and polarization is stronger in groups that are faster and
  - density is more frontal in groups that are larger, and in groups that are slower.
— Greater variability of speed is associated with the following traits: the shape of the group is more oblong and more stable during turning, and the highest density is more frontal.
— When density is sufficiently high, the blind angle is positively correlated with the bearing angle. Empirically we may imagine that in different species of fish with the same eye morphology, the blind angle is smaller when fish undulate than when they are pectoral swimmers and decreases with the amplitude of the head movement. Similarly for birds, the size of the blind angle may depend not only on that of the visual field [85], but also on the frequency of head movement [63,86].
— Bearing angles are similar in groups of different numbers of group members.

Because individuals in these models of swarming are merely a sketch of what real animals are, these models need extensions in future. For instance, they may be extended with variation in behaviour among individuals. Such variation may influence the internal structure of the group, as shown for models of primates [87]. Here, variation in dominance (tendency to win a fight) results in an internal structure with centrality of dominants [88]. Besides, variation in velocity in models of traffic of pedestrians and cars leads to combustion [89,90]. Individuals in these models may be extended with other motivations beyond movement and coordination, such as spawning behaviour [91] and predator avoidance [20,92–94]. These additional motivations have been shown to be of great influence on internal structure and group shape.

Rules of our models have been biologically inspired, but are a strong simplification. For instance, in our flocking model [5,47], flying is represented by fixed-wing aerodynamics and vision by a vision cone [15,26]. It will be interesting to represent in future these aspects in more detail.

Already in its present form, this modelling procedure leads to an integrative approach to collective behaviour. It shows that patterns at the level of the group that resemble empirical data emerge by self-organization from local, behavioural interactions among individuals. Herewith, it increases our understanding of empirical data, and it is a good starting point for further empirical studies.

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